Problem Set 6a

EC404 Spring 2025

[Due, with Part b, on May 1st]

Question 1:

This question asks you to extend the medical-test example from class. Suppose there is a medical condition that afflicts 20% of the population. There is a test for this condition, and the reliability of this test can be characterized as follows:

• false-positive rate = 10% — for those who do not have the condition, 10% will test positive.

• false-negative rate = 5% — for those who have the condition, 5% will test negative.

(a) If you receive a positive test result, what is the likelihood that you have the condition?If you receive a negative test result, what is the likelihood that you do not have the condition?

(b) Repeat part (a), except now assume that the false-positive rate is 5% and the false-negative rate is 10%.

Question 2:

Suppose there are two types of dice, red dice and blue dice. Each red die has 4 H's and 2 M's, whereas each blue die has 2 H's and 4 M's. The proportion of all dice that are red is 80%.

For each of the scenarios below, discuss whether the person's intuitive judgment is consistent with (i) base-rate neglect, (ii) over-inference from small samples, and (iii) conservatism.

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(a) A person is told that a die was rolled three times and came up MMH. When asked the likelihood that the die is red, the person responds 1/2.

(b) A person is told that a die was rolled three times and came up *HMH*. When asked the likelihood that the die is red, the person responds 9/10.

(c) A person is told that a die was rolled ten times and came up *MMHHMHMHHH*. When asked the likelihood that the die is red, the person responds 17/20.

Question 3:

Suppose there are two types of coins, heads-biased coins and tails-biased coins. A heads-biased coin has a 3/4 probability of a heads, while a tails-biased coin has a 1/4 probability of heads. The proportion of all coins that are heads-biased is 1/7.

Suppose that we flip a coin twice and it comes up *HH*.

(a) For a standard Bayesian information processor:

(i) What is the person's posterior probability that the coin is heads-biased?

(ii) What is the person's forecast for a third flip being H?

(b) For an (N = 8)-Freddy (as defined in class):

(i) What is the person's posterior probability that the coin is heads-biased?

(ii) What is the person's forecast for a third flip being H?

(c) Repeat parts (a) and (b) when the proportion of all coins that are heads-biased is 6/7.

(d) How do Freddy's forecasts compare to a Bayesian's forecasts? Provide some intuition for your conclusions.