# Lecture 4: Learning and Information 

Part A: Bayesian Information Processing

EC 404: Behavioral Economics<br>Professor: Ben Bushong

April 2, 2024

## Learning, Experiences, and Information Processing

Many interesting questions in economics involve making inferences when you receive some information about something/someone, you must process that information to infer something about the underlying type.

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After taking a test drive, you must decide whether you have found a
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## Linda the Bank Teller

Linda is 31 years old, single, outspoken, and very bright. She majored in philosophy. As a student, she was deeply concerned with issues of discrimination and social justice, and also participated in anti-nuclear demonstrations. Which is more probable?

Linda is a bank teller

Linda is a bank teller and is active in the feminist movement

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A : Linda is a bank teller.

B : Linda is a bank teller and is active in the feminist movement.

## The Standard Model: Bayesian Information Processing

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Piece 1: Defining types and outcomes

Piece 2: Forecasts given uncertainty over underlying types.

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Let $p(x \mid t)$ denote the probability of outcome $x \in X$ given type $t \in T$

Example A: Suppose there are two dice, a red one and a blue one. On
each die, there are two possible outcomes, $H$ or $M$. However, on the red
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In Example A: $T \equiv\{$ red, blue $\} \quad X \equiv\{H, M\}$

$$
\begin{array}{ll}
p(H \mid \text { red })=2 / 3 & p(H \mid \text { blue })=1 / 3 \\
p(M \mid \text { red })=1 / 3 & p(M \mid \text { blue })=2 / 3
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## Piece 2: Forecasts given uncertainty over underlying types

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Example B: The underlying types are as in Example A. But suppose I flip a fair coin, and if it comes up heads I'll use the red die, and if it comes up tails I'll use the blue die (and you cannot observe the coin flip). What is the likelihood that the die rolled will come up $H$ ?

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In Example B: $q($ red $)=1 / 2$ and $q($ blue $)=1 / 2$, and so

$$
\begin{aligned}
\pi(H) & =q(\text { red }) p(H \mid \text { red }) \\
& =\quad(1 / 2)(2 / 3)+q(\text { blue }) p(H \mid \text { blue }) \\
& +\quad(1 / 2)(1 / 3) \quad=1 / 2
\end{aligned}
$$

## Piece 3: Inferences over types given some information

Let $\phi$ be a signal (a bit of information).
Let $\gamma(\phi \mid t)$ be the probability of signal $\phi$ given type $t \in T$
Let $q_{0}(t)$ denote the prior probability of type $t \in T$ (your prior beliefs about the distribution of types)

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Bayes' rule:

$$
q_{1}(t \mid \phi)=\frac{\gamma(\phi \mid t) q_{0}(t)}{\sum_{t^{\prime} \in T} \gamma\left(\phi \mid t^{\prime}\right) q_{0}\left(t^{\prime}\right)}
$$

## Piece 3: Inferences over types given some information

Example C: The underlying types are as in Example A, and I flip a coin to pick a die as in Example B. But now I roll that die twice and tell you (truthfully) that the die came up HH. What is the likelihood that I'm rolling the red die?

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Example C: The underlying types are as in Example A, and I flip a coin to pick a die as in Example B. But now I roll that die twice and tell you (truthfully) that the die came up HH . What is the likelihood that I'm rolling the red die?

In Example C: $\quad \gamma(H H \mid$ red $)=(2 / 3)(2 / 3)=4 / 9$

$$
\gamma(H H \mid \text { blue })=(1 / 3)(1 / 3)=1 / 9
$$

Hence:

$$
\begin{aligned}
q_{1}(\text { red } \mid H H) & =\frac{\gamma(H H \mid \text { red }) q_{0}(\text { red })}{\gamma(H H \mid \text { red }) q_{0}(\text { red })+\gamma(H H \mid \text { blue }) q_{0}(\text { blue })} \\
& =\frac{(4 / 9)(1 / 2)}{(4 / 9)(1 / 2)+(1 / 9)(1 / 2)}=4 / 5
\end{aligned}
$$

## Piece 4: Forecasts given revised beliefs about types

Let $\pi(x \mid \phi)$ denote the probability of outcome $x \in X$ after having seen signal $\phi$ (your posterior forecast for the likelihood of outcome $x$ ).
$\pi(H \mid H H)$ $q_{1}($ red $\mid H H) p(H \mid$ red $)+q_{1}($ blue $\mid H H) p(H \mid$ blue $)$

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\pi(H \mid H H) & =q_{1}(\text { red } \mid H H) p(H \mid \text { red })+q_{1}(\text { blue } \mid H H) p(H \mid \text { blue }) \\
& =(4 / 5)(2 / 3)+(1 / 5)(1 / 3)=3 / 5
\end{aligned}
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## Example: A Medical Test

Suppose there is a rare disease that afflicts $0.01 \%$ of the population. You were recently tested for this disease, and your test result was positive. The test is $99 \%$ accurate - if you have the disease you will test positive 99 times out of a 100, and if you do not have the disease you will test negative 99 times out of a 100. What is the likelihood that you have the disease?
sick) $q_{0}($ sick $)+\gamma(+\mid$ healthy $) q_{0}$ (healthy)
$\square$

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Note: $\quad q_{0}($ sick $)=0.0001$ and $q_{0}($ healthy $)=0.9999$.

$$
\gamma(+\mid \text { sick })=0.99 \text { and } \gamma(+\mid \text { healthy })=0.01
$$

Hence:

$$
\begin{aligned}
q_{1}(\text { sick } \mid+) & =\frac{\gamma(+\mid \text { sick }) q_{0}(\text { sick })}{\gamma(+\mid \text { sick }) q_{0}(\text { sick })+\gamma(+\mid \text { healthy }) q_{0}(\text { healthy })} \\
& =\frac{(0.99)(0.0001)}{(0.99)(0.0001)+(0.01)(0.9999)}=0.0098=0.98 \%
\end{aligned}
$$

Note: If two positive tests: $q_{1}($ sick $\mid++)=49.5 \%$.

## Example: Financial Analyst

Financial analysts predict whether the market will go up or down, and they are sometimes correct and sometimes incorrect. Moreover, there are good analysts and bad analysts. Good analysts are correct $80 \%$ of the time, while bad analysts are correct $50 \%$ of the time. There are very few good analysts - only $10 \%$ of all analysts are good.

Suppose that you have seen your analyst's predictions for the past two months (and not before), and they have both been correct. This month
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& =\frac{(0.64)(0.1)}{(0.64)(0.1)+(0.25)(0.9)}=0.221 .
\end{aligned}
$$

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Since "market will go down" means "your analyst is correct":


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Step 2: Forecast.
Since "market will go down" means "your analyst is correct":

$$
\begin{aligned}
\pi(H \mid H H) & =q_{1}(\operatorname{good} \mid H H) p(H \mid \operatorname{good})+q_{1}(\operatorname{bad} \mid H H) p(H \mid \operatorname{bad}) \\
& =(0.221) *(0.8)+(0.779) *(0.5)=0.566
\end{aligned}
$$

## (Counter) Example: Information Cascades

I live in a cul-de-sac in a quiet neighborhood. Every week, I forget which day is garbage day. My neighbors also make the same mistake. We all use each other's behavior to infer garbage day-if you see a bunch of trash cans out, then it's probably time to take out the trash.

Suppose that each of us receives some (private) signal that is accurate $2 / 3$ of the time, and this is common knowledge. Suppose we put out our trash sequentially.

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## Seven (+1) Mistakes in Information Processing

We'll work through seven different mistakes that people make in information processing.

This is not a complete list, and it omits one mistake about other people: cursedness. A person's actions reveal something about their private information (see previous example)

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- Selling a used car.
- Buying a stock.

Question: Do people correctly learn that this very action reveals something about their private information?

If not, we say the person is cursed (terminology from Rabin and Eyster).

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## (1) "Base-Rate Neglect"

"Base-rate neglect":

- People tend to pay too little attention to base rates (priors).


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Recall: Bayes' rule is

$$
q_{1}(t \mid \phi)=\frac{\gamma(\phi \mid t) q_{0}(t)}{\sum_{t^{\prime} \in T} \gamma\left(\phi \mid t^{\prime}\right) q_{0}\left(t^{\prime}\right)}
$$

$q_{0}(t)$ is the base rate or prior.

## (1) "Base-Rate Neglect"

## Example [Kahneman \& Tversky (ORIRM 1972)]

A cab was involved in a hit and run accident at night. Two cab companies, the Green and the Blue, operate in the city. You are given the following data

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## Example [Kahneman \& Tversky (ORIRM 1972)]

A cab was involved in a hit and run accident at night. Two cab companies, the Green and the Blue, operate in the city. You are given the following data:
(a) 85 percent of the cabs in the city are Green and 15 percent are Blue.
(b) a witness identified the cab as Blue.

The court tested the reliability of the witness under the same
circumstances that existed on the night of the accident and concluded
that the witness correctly identified each one of the two colors $80 \%$ of
involved in the accident was Blue rather than Green?

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Median answer by subjects was $80 \%$

## The correct Bayesian posterior is $41.4 \%$.

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$$
\begin{aligned}
q_{1}(B \mid b) & =\frac{\gamma(b \mid B) q_{0}(B)}{\gamma(b \mid B) q_{0}(B)+\gamma(b \mid G) q_{0}(G)} \\
& =\frac{(.8)(.15)}{(.8)(.15)+(.2)(.85)}=0.414
\end{aligned}
$$

## (1) "Base-Rate Neglect"

Let $\hat{q}_{1}(t \mid \phi)$ denote a person's reported posterior.
Definition: A person exhibits full base-rate neglect when her reported posterior $\hat{q}_{1}(t \mid \phi)$ is consistent with incorrectly using a uniform prior $\left(q_{0}(t)\right.$ is the same for all $\left.t\right)$, which means

[^0]
## (1) "Base-Rate Neglect"

Let $\hat{q}_{1}(t \mid \phi)$ denote a person's reported posterior.
Definition: A person exhibits full base-rate neglect when her reported posterior $\hat{q}_{1}(t \mid \phi)$ is consistent with incorrectly using a uniform prior ( $q_{0}(t)$ is the same for all $t$ ), which means

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Common Result: When the sample is more "representative" of one cage than the other, there is over-inference toward that cage.

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Player-by-player statistics from the 1980-81 76ers:

| $\operatorname{Pr}(H \mid M M M)$ | $\operatorname{Pr}(H \mid M M)$ | $\operatorname{Pr}(H)$ | $\operatorname{Pr}(H \mid H H)$ | $\operatorname{Pr}(H \mid H H H)$ |
| :---: | :---: | :---: | :---: | :---: |
| . 50 | . 47 | . 50 | . 50 | . 48 |
| . 52 | . 51 | . 52 | . 52 | . 48 |
| . 50 | . 49 | . 46 | . 46 | . 32 |
| . 77 | . 60 | . 56 | . 54 | . 59 |
| . 50 | . 48 | . 47 | . 43 | . 27 |
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- People tend to be too conservative in making inferences. Edwards (1968) finds opposite results from the over-inference studies that people don't update enough from the samples. Definition: A person exhibits under-inference (or conservatism) when her reported posterior $\hat{q}_{1}(t \mid \phi)$ is such that:


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More generally, people seem to have a lack of understanding of randomness.

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(2) Availability heuristic (salience): People evaluate the probability of event $A$ by the ease with which instances and occurrences can be brought to mind.
(3) Anchoring-and-adjustment heuristic: People make judgments by starting from some initial value and then making adjustments, but the adjustments are typically insufficient (Slovic and Lichtenstein, OBHP 1971).


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