Lecture 4: Learning and Information Part A: Bayesian Information Processing

EC 404: Behavioral Economics Professor: Ben Bushong

April 2, 2024

Many interesting questions in economics involve making *inferences* — when you receive some information about something/someone, you must process that information to infer something about the underlying type.

- After observing a stock's recent performance, you must decide whether it is a good vs. bad stock to invest in.
- After taking a test drive, you must decide whether you have found a good vs. bad car.
- After interviewing a person, you must decide whether she is a good vs. bad job candidate.
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Linda is 31 years old, single, outspoken, and very bright. She majored in philosophy. As a student, she was deeply concerned with issues of discrimination and social justice, and also participated in anti-nuclear demonstrations. Which is more probable?

A : Linda is a bank teller.

B : Linda is a bank teller and is active in the feminist movement.

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Let T denote a set of underlying types.

Let X denote a set of outcomes.

Let p(x|t) denote the probability of outcome $x \in X$ given type $t \in T$.

Example A: Suppose there are two dice, a red one and a blue one. On each die, there are two possible outcomes, *H* or *M*. However, on the red die, there are 4 *H*'s and 2 *M*'s, whereas on the blue die, there are 2 *H*'s and 4 *M*'s.

In Example A: $T \equiv \{ \text{ red }, \text{ blue } \}$ $X \equiv \{ H, M \}$ p(H|red) = 2/3 p(H|blue) = 1/3

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Let q(t) denote the probability of type $t \in T$ (your beliefs about the distribution of underlying types).

Let $\pi(x)$ denote the probability of outcome $x \in X$ (your forecast for the likelihood of outcome x).

$$\pi(x) = \sum_{t\in T} [q(t) p(x|t)].$$

Example B: The underlying types are as in Example A. But suppose I flip a fair coin, and if it comes up heads I'll use the red die, and if it comes up tails I'll use the blue die (and you cannot observe the coin flip). What is the likelihood that the die rolled will come up *H*?

$$\begin{aligned} \pi(H) &= q(\text{red}) \ p(H|\text{red}) \ + \ q(\text{blue}) \ p(H|\text{blue}) \\ &= (1/2)(2/3) \ + \ (1/2)(1/3) \ = 1, \end{aligned}$$

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In Example B: q(red) = 1/2 and q(blue) = 1/2, and so $\pi(H) = q(red) p(H|red) + q(blue) p(H|blue)$ = (1/2)(2/3) + (1/2)(1/3) = 1/2

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Let $\gamma(\phi|t)$ be the probability of signal ϕ given type $t \in \mathcal{T}$.

Let $q_0(t)$ denote the *prior probability* of type $t \in T$ (your prior beliefs about the distribution of types).

Let $q_1(t|\phi)$ denote the *posterior probability* of type $t \in T$ after having seen signal ϕ (your posterior beliefs about the distribution of types). Baves' rule:

$$q_1(t|\phi) = \frac{\gamma(\phi|t)q_0(t)}{\sum_{t'\in\mathcal{T}}\gamma(\phi|t')q_0(t')}$$

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Piece 3: Inferences over types given some information

Example C: The underlying types are as in Example A, and I flip a coin to pick a die as in Example B. But now I roll that die twice and tell you (truthfully) that the die came up *HH*. What is the likelihood that I'm rolling the red die?

In Example C: $\gamma(HH|red) = (2/3)(2/3) = 4/9$

 $\gamma(HH|blue) = (1/3)(1/3) = 1/9$

Hence:

$$q_{1}(\text{red}|HH) = \frac{\gamma(HH|\text{red})q_{0}(\text{red})}{\gamma(HH|\text{red})q_{0}(\text{red}) + \gamma(HH|\text{blue})q_{0}(\text{blue})}$$
$$= \frac{(4/9)(1/2)}{(4/9)(1/2) + (1/9)(1/2)} = 4/5.$$

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Piece 4: Forecasts given revised beliefs about types

Let $\pi(x|\phi)$ denote the probability of outcome $x \in X$ after having seen signal ϕ (your posterior forecast for the likelihood of outcome x).

$$\pi(x|\phi) = \sum_{t\in\mathcal{T}} \left[q_1(t|\phi) \ p(x|t)\right].$$

In Example C:

 $\pi(H|HH) = q_1(red|HH) p(H|red) + q_1(blue|HH) p(H|blue)$

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Example: A Medical Test

Suppose there is a rare disease that afflicts 0.01% of the population. You were recently tested for this disease, and your test result was positive. The test is 99% accurate — if you have the disease you will test positive 99 times out of a 100, and if you do not have the disease you will test negative 99 times out of a 100. What is the likelihood that you have the disease?

Note:
$$q_0(\text{sick}) = 0.0001$$
 and $q_0(\text{healthy}) = 0.9999$.
 $\gamma(+|\text{sick}) = 0.99$ and $\gamma(+|\text{healthy}) = 0.01$.

Hence:

$$q_{1}(\text{sick}|+) = \frac{\gamma(+|\text{sick})q_{0}(\text{sick})}{\gamma(+|\text{sick})q_{0}(\text{sick}) + \gamma(+|\text{healthy})q_{0}(\text{healthy})}$$
$$= \frac{(0.99)(0.0001)}{(0.99)(0.0001) + (0.01)(0.9999)} = 0.0098 = 0.98\%.$$

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Financial analysts predict whether the market will go up or down, and they are sometimes correct and sometimes incorrect. Moreover, there are good analysts and bad analysts. Good analysts are correct 80% of the time, while bad analysts are correct 50% of the time. There are very few good analysts — only 10% of all analysts are good.

Suppose that you have seen your analyst's predictions for the past two months (and not before), and they have both been correct. This month, your analyst is predicting that the market will go down. What should you believe is the likelihood that the market will go down? Financial analysts predict whether the market will go up or down, and they are sometimes correct and sometimes incorrect. Moreover, there are good analysts and bad analysts. Good analysts are correct 80% of the time, while bad analysts are correct 50% of the time. There are very few good analysts — only 10% of all analysts are good.

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$$q_{1}(\text{good}|HH) = \frac{\gamma(HH|\text{good})q_{0}(\text{good})}{\gamma(HH|\text{good})q_{0}(\text{good}) + \gamma(HH|\text{bad})q_{0}(\text{bad})}$$
$$= \frac{(0.64)(0.1)}{(0.64)(0.1) + (0.25)(0.9)} = 0.221.$$

Step 2: Forecast.

Since "market will go down" means "your analyst is correct":

 $\pi(H|HH) = q_1(\text{good}|HH)p(H|\text{good}) + q_1(\text{bad}|HH)p(H|\text{bad})$

= (0.221) * (0.8) + (0.779) * (0.5) = 0.566.

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I live in a cul-de-sac in a quiet neighborhood. Every week, I forget which day is garbage day. My neighbors also make the same mistake. We all use each other's behavior to infer garbage day—if you see a bunch of trash cans out, then it's probably time to take out the trash.

Suppose that each of us receives some (private) signal that is accurate 2/3 of the time, and this is common knowledge. Suppose we put out our trash sequentially.

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We'll work through seven different mistakes that people make in information processing.

This is not a complete list, and it omits one mistake about other people: *cursedness*.

A person's actions reveal something about their private information (see previous example).

- Selling a used car.
- Buying a stock.
- ► Offering a product for sale at all.

Question: Do people correctly learn that this very action reveals something about their private information?

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"Base-rate neglect":

▶ People tend to pay too little attention to base rates (priors).

Recall: Bayes' rule is

$$q_1(t|\phi) = rac{\gamma(\phi|t)q_0(t)}{\sum_{t'\in\mathcal{T}}\gamma(\phi|t')q_0(t')}$$

 $q_0(t)$ is the base rate or prior.

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$$q_1(t|\phi) = rac{\gamma(\phi|t)q_0(t)}{\sum_{t'\in\mathcal{T}}\gamma(\phi|t')q_0(t')}$$

 $q_0(t)$ is the base rate or prior.

A cab was involved in a hit and run accident at night. Two cab companies, the Green and the Blue, operate in the city. You are given the following data:

(a) 85 percent of the cabs in the city are Green and 15 percent are Blue.

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Median answer by subjects was 80%

The correct Bayesian posterior is 41.4%.

$$\begin{aligned} q_1(B|b) &= \frac{\gamma(b|B)q_0(B)}{\gamma(b|B)q_0(B) + \gamma(b|G)q_0(G)} \\ &= \frac{(.8)(.15)}{(.8)(.15) + (.2)(.85)} = 0.414 \end{aligned}$$

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Let $\hat{q}_1(t|\phi)$ denote a person's reported posterior.

Definition: A person exhibits *full base-rate neglect* when her reported posterior $\hat{q}_1(t|\phi)$ is consistent with incorrectly using a uniform prior $(q_0(t) \text{ is the same for all } t)$, which means

$$\hat{q}_1(t|\phi) = \frac{\gamma(\phi|t)}{\sum_{t'\in\mathcal{T}}\gamma(\phi|t')} \equiv q_1^{BRN}(t|\phi).$$

Recall: The correct Bayesian posterior is:

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"Law of Small Numbers":

People tend to exaggerate the degree to which a small sample will resemble the underlying population.

Example [Kahneman & Tversky (Cog. Psych. 1972)]

A certain town is served by two hospitals. In the larger hospital about 45 babies are born each day, and in the smaller hospital about 15 babies are born each day. As you know, about 50% of all babies are boys. The exact percentage of baby boys, however, varies from day to day. Sometimes it may be higher than 50%, sometimes lower.

For a period of 1 year, each hospital recorded the days on which more than 60% of the babies born were boys. Which hospital do you think recorded more such days?

<u>Result</u>: 22% answered the larger hospital, 56% answered about the same (within 5% of each other), and only 22% answered the small hospital.

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- Roulette: "Black is due."
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Duration since number last chosen:	Number	Mean Winnings
< 1 week:	8	\$349
1 and 2 weeks:	8	\$349
2 and 3 weeks:	14	\$308
3 and 8 weeks:	59	\$301
> 8 weeks:	1622	\$260
All winners:	1714	\$262

"Over-inference from small samples":

People tend to infer too much about an underlying probability process from a small sample.

Common procedure [from Grether (*QJE* 1980)]:

- Step 1: Draw a ball from Cage X to determine whether Cage A or Cage B will subsequently be used.
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"Hot-hand fallacy":

The tendency to perceive positive autocorrelation (a "hot hand") in i.i.d. sequences.

Having hot & cold streaks means something like:

 $\Pr(H|HHH), \Pr(H|HH) > \Pr(H|MM), \Pr(H|MMM).$

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Player-by-player statistics from the 1980-81 76ers:						
Pr(<i>H</i> <i>MMM</i>)	Pr(<i>H</i> <i>MM</i>)	$\Pr(H)$	Pr(<i>H</i> ∣ <i>HH</i>)	Pr(<i>H</i> ∣ <i>HHH</i>)		
.50	.47	.50	.50	.48		
.52	.51	.52	.52	.48		
.50	.49	.46	.46	.32		
.77	.60	.56	.54	.59		
.50	.48	.47	.43	.27		
.52	.53	.46	.40	.34		
.61	.58	.54	.47	.53		
.70	.56	.52	.48	.36		
.88	.73	.62	.58	.51		

People tend to be too conservative in making inferences.

Edwards (1968) finds opposite results from the over-inference studies – that people don't update enough from the samples.

Definition: A person exhibits *under-inference* (or *conservatism*) when her reported posterior $\hat{q}_1(t|\phi)$ is such that:

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Over-inference from small samples vs. conservatism — how to resolve?

Griffin & Tversky (1992) suggest that people focus too much on the *strength* of evidence and too little on the *weight* of evidence.

- Conservatism studies present people with low-strength/high-weight signals (large samples with relatively even distributions of H vs. M).
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More generally, people seem to have a lack of understanding of randomness.

• Which birth order is more likely in a family with six children:

GBGBBG vs. BGBBBB

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Suppose there are 23 people in a room — what's the likelihood that there are two people that share a birthday?

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(2) Availability heuristic (salience): People evaluate the probability of event A by the ease with which instances and occurrences can be brought to mind.

(3) <u>Anchoring-and-adjustment heuristic</u>: People make judgments by starting from some initial value and then making adjustments, but the adjustments are typically insufficient (Slovic and Lichtenstein, *OBHP* 1971).